Resection

The last newsletter focused on the basic principles of Resection and the least squares methods that are applied in this setup method. This newsletter is again about Resection but gives much more detail about the applied mathematical models.

As explained in the last newsletter the Resection method allows some or all of the following parameters to be computed and set:

- 2D position of station
- Height of station
- Orientation
- Scale factor

Computation of these parameters can be done using either the regular least squares adjustment or the so-called robust calculation. Before looking in detail at these methods some important points common to both methods should be explained.

Target Point Accuracy

A resection uses measurements of up to ten target points to calculate the parameters mentioned above. These target points may be 3D, 2D or height-only points. The estimated accuracy (that is, the “reliability”) of the target points can be defined in the SETUP Configuration panel:

- 2D position of station
- Height of station
- Orientation
- Scale factor

These estimated accuracies are then used in the least squares adjustment calculation to construct realistic weight information for the observations.

Calculations

The principle aim of the calculations is to use all available data to determine the results whilst also identifying any possible errors.

Least Squares / Robust Adjustment

It is possible to choose between using the Least Squares and Robust calculation methods in the SETUP Results panel.

Least Squares Method:

- The weight (or standard deviation) which is assigned to each observation is composed of a constant and a variable part.
- The constant part depends on the pre-defined angular and EDM accuracies of the instrument.
- The variable part is computed from the accuracy of the target points (as defined earlier in the SETUP Configuration panel) and the distance between target point and station.

Weighting

Both methods actually use least squares computations but for the Robust method a modified form of the general principle of least-squares adjustment is applied – in simplest terms, the least-squares technique is adopted with “robust weighting”.

This difference is explained in more detail below.

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Robust Method: Rather than applying weights to observations as described above, weights are calculated depending on the fit between the observed and the computed value for an observation. Therefore, observations which are in good agreement with the computed values are awarded higher weights relative to those which have large differences between observed and computed values.

The advantage of the robust weighting is that it enables good results to be obtained even if errors are within the data. Bad data is effectively “de-weighted” and therefore has little or no influence upon the results.

Note, if all measurements are of high quality the results for the robust method will be consistent with the results of the least squares method.

DETERMINATION OF PROVISIONAL VALUES

Using the available target point coordinates and measurements, various geometrical routines are used to compute “provisional” easting/northing co-ordinates from unique combinations of the data. Various checks are applied to ensure that “chance” solutions are excluded.

Having identified a group of results which contain the best potential provisional values, the median values are determined. Theoretically, any result within this group should be suitable, however, a median value is taken to add extra confidence to the selection. This also helps to avoid selection of a value, which is not in agreement with the rest of the values.

The procedure for determining provisional values for height is more straightforward as only one observation needs to be considered at a time. Again the median height value from the set of provisional values is selected as the best provisional value to use.

The approach described for determining the provisional values is very reliable but is limited by the available redundancy and the percentage of errors in the data. As the redundancy falls and the percentage of errors increases so the likelihood of obtaining good provisional values decreases.

ITERATING TO THE RESULT

Once weights for all observations and provisional values for the results are available the least squares adjustment routines can be started.

When performing a resection computation up to five parameters may be determined - easting, northing, height, orientation and scale factor. The calculation of the final results may require a number of iterations until the change in the computed parameters are no longer significant – this is when changes in the values are less than the set criteria listed below.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Criteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>Easting</td>
<td>0.5mm</td>
</tr>
<tr>
<td>Northing</td>
<td>0.5mm</td>
</tr>
<tr>
<td>Orientation</td>
<td>2&quot;</td>
</tr>
<tr>
<td>Scale factor</td>
<td>See below</td>
</tr>
<tr>
<td>Height</td>
<td>0.5mm</td>
</tr>
</tbody>
</table>

The scale factor criterion is a function of the positional accuracy of the target points and the maximum distance measurement. For example, if an accuracy of 10mm has been specified and distances up to 1000m have been measured, then the resulting scale factor must be determined to 10ppm.

PUTTING IT INTO PRACTICE – AN EXAMPLE

Below is an example to illustrate the effect of using the different methods

Imagine four target points arranged in a square with a side length of 100m. The TPS instrument is set up roughly in the centre and it is necessary to determine the coordinates of the setup using a resection.

Unfortunately for the surveyor, the chainman has set up the reflector at P2 on the wrong point – it has been setup over a point which actually has the coordinates (96,98,100).

The surveyor does not realise this and starts the resection routine and measures angles and distances to the 4 points.

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After measuring the 4th point he presses F5(CALC) to compute the resection and view the results.

Immediately after pressing F5(CALC) (and before the results are shown) a series of warnings inform the surveyor that the positional accuracy and orientation accuracy were not achieved. The surveyor acknowledges these warning messages and then the SETUP Results panel Stn Coords page view is shown.

In order to check the quality of the results the surveyor accesses the Sigma page view – it now starts to become obvious that something is wrong. The standard deviations and scale factor are far too big.

The surveyor decides to investigate this in more detail and looks at the residuals of the individual observations by pressing F4(INFO) to access the SETUP Additional Information panel.

On initial inspection, the surveyor may think that since the dHz residual value to P1 is the biggest then there must be something wrong with the measurement to P1 or with the control coordinates of P1.

But looking closer it can be seen that the ! mark in the left-most column indicates that there may actually be something wrong with the measurements to P2.

It should be remembered that a gross error in any observation affects the residuals of all observations - but it is not necessarily the observation with the biggest residual that contains the error.

The surveyor presses the F5(MORE) button which changes the right-most column to display the residuals for the dDist observations.

It is now clearer to the surveyor where the error may lay...

But for now the surveyor presses ESC to return to the SETUP Results panel and changes to the robust calculation by pressing F3(ROBST).
The results (easting and northing of the station) are very different from the ones in the least squares results panel – and a look at the Sigma page view confirms this. The standard deviations are much smaller and the calculated scale is more realistic. The surveyor presses F5(INFO) again to view more detailed information about the residuals of the individual observations for Hz …

There is now no doubt in the surveyor’s mind as to which observation is at fault and can investigate further.

It can now be seen that due to the different weighting mechanisms used in the robust method, the wrong observation to P2 was detected and “de-weighted” to such an extent such that its influence on the result is practically zero.

In order to get a “clean” result the surveyor now has 3 options:

1. Disable observation P2 for the calculation by pressing the F3(USE) button until Use is set to No and then press F1(RECLC). This keeps the observation in the database, but does not use it for the calculation of the result

2. Completely remove the observation by pressing F4(REMOV). This also deletes the measurement permanently from the job.

3. Return to SETUP Results panel and press F5(SURVV) to re-measure point P2 (assuming the chainman has managed to set the reflector over the correct point this time)

**Final Hint**

Once the surveyor had excluded the wrong measurement from the calculation, then both methods (least squares and robust) will deliver the same result.

This means that the two methods can be used to quickly check the “robustness” of the resection. Once in the results panel simply toggle between the two methods and check if the result changes. If the results are very similar then the resection result should be acceptable. If it does change then it maybe worth to investigate further and have a closer look at the residuals.

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